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DOI: <https://doi.org/10.3390/inorganics7060073>

Posted at the Zurich Open Repository and Archive, University of Zurich

ZORA URL: <https://doi.org/10.5167/uzh-183181>

Journal Article

Published Version



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Originally published at:

Schilling, Mauro; Lubner, Sandra (2019). Determination of pKa Values via ab initio Molecular Dynamics and its Application to Transition Metal-Based Water Oxidation Catalysts. *Inorganics*, 7(6):73.

DOI: <https://doi.org/10.3390/inorganics7060073>

Article

Determination of pK_a Values via *ab initio* Molecular Dynamics and its Application to Transition Metal-Based Water Oxidation Catalysts

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Received: 11 May 2019; Accepted: 6 June 2019; Published: 12 June 2019



Abstract: The pK_a values are important for the in-depth elucidation of catalytic processes, the computational determination of which has been challenging. The first simulation protocols employing *ab initio* molecular dynamics simulations to calculate pK_a values appeared almost two decades ago. Since then several slightly different methods have been proposed. We compare the performance of various evaluation methods in order to determine the most reliable protocol when it comes to simulate pK_a values of transition metal-based complexes, such as the here investigated Ru-based water oxidation catalysts. The latter are of high interest for sustainable solar-light driven water splitting, and understanding of the underlying reaction mechanism is crucial for their further development.

Keywords: bluemoon; *ab initio* molecular dynamics; pK_a ; density functional theory; water splitting

1. Introduction

Nowadays, transition metal-based catalysts are employed for a broad range of applications including pharmaceuticals, industrial scale synthesis and the development of renewable energy sources. Among the latter is the class of water-splitting catalysts that is subdivided into water oxidation catalysts which oxidize water and evolve molecular oxygen, and water reduction catalysts, which reduce protons in order to release molecular hydrogen. Analogously to nature's photosynthesis process, the goal of those catalysts is either to oxidize water to molecular oxygen thereby generating reduction equivalents or to use the latter to form energy rich chemical bonds, for example in the form of molecular hydrogen.

An in-depth understanding of the underlying reaction mechanisms for those processes is crucial in order to further improve or rationally design novel catalysts. A prerequisite for mechanistic studies is the knowledge of the chemical speciation of the transition metal complex under catalytic conditions. When working under aqueous conditions, special attention has to be given to functional groups which might undergo protonation/deprotonation reactions. Unfortunately it is often difficult to determine physical properties such as acidity constants (pK_a) of catalytic intermediates due to their elusive nature. In this study we apply density functional theory (DFT)-based molecular dynamics, so-called *ab initio* molecular dynamics (AIMD), to reliably determine pK_a values of transition metal complexes used as catalysts for water oxidation. The here discussed methodologies have been successfully applied to a variety of compounds up to now, among them are organic molecules [1–3], amino acids and peptides [4,5] as well as aqua complexes of transition metals [6].

While all the studies mentioned above are based on the same protocol, namely the Bluemoon methodology, there are significant differences when it comes to the post-processing. In the following

we will shortly introduce the general protocol, as well as the different flavors of post-processing. Then we compare those approaches for a set of benchmarking molecules, as well as for the system of interest—a ruthenium-based water oxidation catalyst $[\text{Ru}(\text{II})\text{Py}_5\text{OMe}(\text{OH}_2)]^{2+}$ (where $\text{Py}_5\text{OMe} = 6,6''\text{-(methoxy(pyridin-2-yl)methylene)di-2,2'-bipyridine}$) [7]. The said system, and in particular the thermodynamics and kinetics of the water oxidation process, were already investigated in-depth by Lubner and co-workers employing DFT simulations [7,8]. Those studies gave important insights with respect to the water oxidation mechanism and further helped to come up with some design guidelines on how to further improve those catalysts. However, the limitations imposed by the implicit solvation led to the desire for a more sophisticated description of the solvation shell. In this context, also this study serves as a mini-review and benchmark study to validate the methodology for pK_a determination to be applied to the same or similar systems in the future.

2. Methodology

The calculation of pK_a values is a common task in computational chemistry—it is therefore not surprising that there are many protocols available for various levels of theory [9]. The most common approach used for small molecules is based on the calculation of the difference in free energy between the protonated and the deprotonated species using a thermodynamic cycle scheme, whereby the interaction between the solvent and solute was approximated by an electrostatic potential by means of an implicit solvation model [10,11]. Alternatively, the electrostatic contribution of solvation can be obtained in a two-step procedure. In the first step, the point charge distribution was generated by the restricted electrostatic potential (RESP) procedure [12]. Then the Poisson equation is solved in order to obtain the electrostatic energies of solvation [13,14]. In combination with sampling of the conformational space, the second approach is in particular useful for large systems such as proteins which possess multiple protonation sites [15,16]. Even though many protocols are able to reliably reproduce experimental pK_a values, their performance is still strongly system dependent. For example, large, flexible or highly charged species stand in conflict with the underlying approximations of some of those protocols. There are numerous protocols and correction schemes depending on the system of interest which can be used to account for such shortcomings. A full review of them is beyond the scope of the current work, and we refer the interested reader to a number of selected articles [17–25].

An obvious approach to improve the previously presented protocol was to describe the solvent at an atomistic level. However, if both the solute and the solvent are treated explicitly using AIMD not only the computational cost rises drastically but also the simulation protocols become more elaborated [26–32].

Among those protocols was the so-called Bluemoon ensemble, where the free energy difference ΔF between the protonated and deprotonated state is calculated by a thermodynamic integration scheme. In this case the integrand is the average force ($f_{\xi'}$) acting on a system to impose the constraint (ξ), while the discrete values of the constraint (ξ') define the range of the integration:

$$\Delta F = - \int_{\xi_0}^{\xi_1} f_{\xi'} d\xi'. \quad (1)$$

The latter is also referred to as potential of mean force (PMF). The average force $f_{\xi'}$ is derived from the Lagrange multiplier λ according to

$$f_{\xi'} = \frac{\langle Z^{-1/2}[\lambda - k_B T G] \rangle_{\xi'}}{\langle Z^{-1/2} \rangle_{\xi'}}, \quad (2)$$

where k_B is the Boltzmann constant, T the temperature, and Z and G are correction factors associated with the transformation from generalized to Cartesian coordinates. In the case of distance constraint ($d(\text{A}-\text{H})$) Equation (2) simplifies to $\langle \lambda \rangle_{\xi'} = f_{\xi'}$.

A detailed derivation of the Bluemoon methodology and in particular Equation (2) can be found in the corresponding original literature by Sprik and Ciccotti [33–35].

The application of the Bluemoon methodology to determine pK_a values is in principle straight forward, however certain aspects deserve attention.

2.1. Choice of Constraint

From a chemical point of view the two states of interest, i.e., the protonated and deprotonated species, are well defined. Either the proton is bound to the acidic functional group (A) or it is (infinitely) far away from the latter stabilized by an extensive hydrogen bonding network. Simulating the deprotonation state in a chemical sense is restricted due to the limitations with regard to the size of the simulation cell. There are sophisticated proton insertion schemes which avoid this problem [3,26–29]. However their high demand in terms of computational resources renders this approach unsuitable for complex systems.

A crucial choice within the Bluemoon methodology is the nature of the constraint that describes the two states. The most simple one is the A–H distance ($d(A-H)$). While it is often applicable, it suffers from some intrinsic problems. First, this constraint does not prevent the re-protonation of the acidic group. Secondly, upon deprotonation, proton hopping might take place from the proton accepting molecule to other solvent molecules according to the Grotthuss mechanism. This is problematic since for large distances, in principle the intermolecular distance between the acidic group and a water molecule somewhere in solution is constraint. The latter is different from simulating a hydronium ion at infinite separation from the acidic group. Besides that, the important question arises at which distance is a covalent O–H bond broken, respectively, which distances have to be sampled in order to reach the deprotonated state. In particular proton hopping makes this decision ambiguous. Nevertheless there are several systems known for which the simple distance constrained turned out to work reasonably well [2,5,36].

Those issues might be circumvented by not only constraining a single A–H bond but the coordination number (CN) of all the protons to the acidic group [37]. The coordination number is commonly represented as the sum over sigmoid functions such as a Fermi–Dirac distribution. The latter has been successfully applied to several systems [1,3,31,32,38].

While a CN prevents the reprotonation of the acidic group it still does not prevent proton hopping. De Meyer et al. resolved this problem by constraining the difference in the CN of all the protons (index i , total number of protons: N) to the acidic group (index j) and a selected solvent molecule (index k) in its proximity:

$$CN(r_{ij}, r_{ik}) = \frac{\sum_i^N (1 - (\frac{r_{ij}}{r_0})^n)}{\sum_i^N (1 - (\frac{r_{ij}}{r_0})^m)} - \frac{\sum_i^N (1 - (\frac{r_{ik}}{r_0})^n)}{\sum_i^N (1 - (\frac{r_{ik}}{r_0})^m)}, \quad (3)$$

where r_{ij} is the length of the vector \vec{r}_{ij} , describing the distance of proton i to the acidic group j , analogously r_{ik} is the distance of proton i to the solvent molecule k . The inflection point is defined by r_0 , and exponential factors n and m define the overall shape of the switch function. This constraint in principle guaranties a smooth transition from the protonated acid to a solvent molecule without further proton hopping [3]. However, the said constraint introduces an additional empirical parameter, namely the choice of the proton accepting solvent molecule. Nonetheless, similar pK_a values were obtained when the accepting molecule was either part of the first or second solvation shell [3].

2.2. Estimation of pK_a Values from the Free Energy Differences

Independent of the constraint used for the simulation, the free energy differences obtained from the Bluemoon ensemble might be interpreted as equilibrium constants from which pK_a values can be determined. There are several proposed ways, all of which have been shown to be able to reproduce experimental results reasonably well. However, to the best of our knowledge, those approaches have not be directly compared for the very same system. In the following we will present the different techniques, highlight their requirements in terms of simulations protocols and the necessary empiric

parameters for the evaluation. For the detailed derivation of those methods, we refer the reader to the indicated references.

2.2.1. Absolute pK_a

The most straight forward approach is to use the relation between the equilibrium constant pK_a and the difference in free energy (ΔF):

$$pK_a = \frac{\beta \Delta F}{\ln(10)}, \quad (4)$$

with $\beta = 1/k_B T$.

In order to reproduce experimental pK_a values one has to assure that the difference in free energy sufficiently describes the two states. This boils down to the nature of the constraint as well as to the range of sampling the corresponding phase space. In any case a key requirement is the convergence of $\Delta F(\xi)$ to a constant value towards the limits of the sampled range (ξ_{min} to ξ_{max}), i.e., $\lim_{\xi \rightarrow \xi_{max}} \Delta F(\xi) = \text{constant}$. Further, in order to obtain meaningful results from the thermodynamic integration the free energy at the bound state $F(\xi_0)$ has to be set to unity. This method has been successfully applied to several systems using either the $d(A-H)-d(O-H)$, the $CN(A-H)$ or $CN(A-H)-CN(O-H)$ (see Equation (3)) constraints [2,3,39].

Whether the calculated free energy difference ΔF can directly be related to the equilibrium constant is disputed in literature [4,6,31]. Authors who disagree with the previously discussed method commonly refer to Chandler's derivations of the equilibrium constant based on a classical statistical mechanical description. The basic principle described there is the relation of the free energy difference ΔF and the radial distribution function (RDF) according to the reversible work theorem [40]. The RDF itself might be interpreted as the probability to find a proton within a certain radius of the acidic group. The probability distribution is related to the (inverse) acidity constant according to [31]:

$$K_a^{-1} = c_0 \int_0^\infty \exp[-\beta \Delta F(r)] 4\pi r^2 dr, \quad (5)$$

where c_0 is the standard concentration. Note the difference in free energy $\Delta F(r)$ is a function of radius of a sphere around the acidic group and not of the constraint ξ . The latter are only equal in case of the distance constraint $d(A-H)$. In principle $\Delta F(r)$ has to be known for infinite separation, in practice however only a finite separation $R_{max} \leq L/2$ (L is the length of the cubic cell simulation) is accessible. Since $\Delta F(r)$ asymptotically approaches a constant value, one often defines $R_c \leq R_{max}$, where R_c is the radius which distinguishes $A-H$ from $A^- + H^+$, i.e., the distance at which the covalent bond is broken [31]. The limitations with respect to the simulation cell result in an uncertainty in the pK_a value which Davies et al. quantified as $\Delta F(R_{max}) / (2.3k_B T)$ [31].

Based on the RDF there are two common approaches to derive pK_a values, both of which require an additional set of simulations in order to reduce the potential errors describe above.

2.2.2. Relative pK_a

The approach presented by Ivanov et al.—in the later referred to as “relative pK_a ”—takes advantage of error-cancellation upon reporting the pK_a value relative to a pK_a value of a reference system (REF):

$$\frac{K_a^{HA}}{K_a^{REF}} = \frac{\int_0^{R_c} \exp[-\beta \Delta F_{REF}(r)] r^2 dr}{\int_0^{R_c} \exp[-\beta \Delta F_{HA}(r)] r^2 dr}. \quad (6)$$

Compared to Equation (5) the integration is from 0 to R_c ($R_c \leq R_{max}$) in order to account for the fact that $\lim_{r \rightarrow R_{max}} pK_a(r)$ asymptotically approaches $pK_a(R_{max})$, i.e., $pK_a(r)$ quickly becomes a constant value [4]. Further, the lower bound of the integral can be approximated by the value slightly smaller

than the average A–H bond length, since the contributions of large values of $-\Delta F(r)$ in the exponent are negligible [4]. The reference system (see Equation (6)) has to be calculated within the same computational framework, which in fact doubles the cost of the approach compared to the previously described method. However, the reference system might be used for the determination of pK_a values of multiple species. Further in order to equate Equation (6), $\Delta F(R_{max})$ is set to unity for both the acid and the reference system [4,5].

This method has been successfully applied to several isomers of histidine as well as a histidine-tryptophan dimer employing a simple d(A–H) constraint [4,5].

2.2.3. Probabilistic pK_a

The second approach was introduced by Davies et al., later referred to as “probabilistic pK_a ” [31]. The main idea is to define the acid dissociation constant K_a by the probabilities to find protons within a certain volume of the acidic group. Then the normalized probability to find a proton within a cutoff radius R_c is

$$P(R_c) = \frac{\int_0^{R_c} \exp[-\beta\Delta F(r)] r^2 dr}{\int_0^{R_{max}} \exp[-\beta\Delta F(r)] r^2 dr}, \quad (7)$$

where R_c is the cutoff radius defining the protonated and the deprotonated state and R_{max} the limit for infinite separation.

In the limit for weak acids the K_a value then becomes

$$K_a(R_c) = \frac{(1 - P(R_c))^2}{P(R_c)} \frac{N}{c_0 V}, \quad (8)$$

where c_0 is the standard concentration, V the volume of the simulation cell and N the number of acidic sides—here $N = 1$. The latter is converted to mol by dividing it by the Avogadro constant.

Here again the choice of the cutoff radius R_c is crucial. However, unlike the relative pK_a scheme, there is no obvious asymptotic behavior within the range of the deprotonation. This led Davies et al. to calculate the pK_w of liquid water using the following relation:

$$K_w(R_c) = \left((1 - P(R_c))^2 \frac{N_w}{c_0 V} \right), \quad (9)$$

where N_w is the number of water molecules in the simulation cell. R_c is the radius at which $pK_w(r) = 14$ is true [31]. The relation between the Equation (8) and (9) is that the activity of the undissociated reactant is set to unity [31].

As for the previous methods, the current one has been successfully applied to several systems employing either a simple d(A–H) constraint or more commonly a CN constraint [1,6,31,32,38].

By introducing the three approaches named “absolute”, “relative” and “probabilistic” pK_a we have laid the foundation for the following study.

3. Computational Settings

AIMD simulations were performed employing the CP2K program package [41]. All atoms were described by the DZVP-MOLOPT-SR-GTH basis sets [42] as well as the corresponding GTH-BLYP pseudo potentials [43]. In order to enlarge the time step the mass of all hydrogen atoms was set to 2 a.m.u. in accordance with literature [3]. The influence of the latter is discussed in Section 4. The BLYP [44,45] exchange-correlation functional together with Grimme’s D3 dispersion correction [46], and a cutoff of 800 Ry for the auxiliary plane wave basis set were used.

In order to simulate liquid water, we used a cubic simulation cell with a side-length of 15.6404 Å containing 128 water molecules. This box size corresponds to liquid water at 1 bar and 300 K using the TIP5P force field [47]. The same simulation cell was used for solvated molecules,

by deleting several water molecules we assured that the pressure remained approximately the same as the one of clean liquid water. For some model systems a larger simulation cell with side-length 19.7340 Å containing 256 water molecules was employed.

The simulations were performed in the NVT ensemble with a time-step of 0.5 fs. The temperature was kept constant at 320 K by a Nosé-Hoover chain thermostat [48,49]. The slightly elevated temperature is required in order to avoid the glassy behavior of BLYP water [50].

The general settings mentioned above closely resemble the protocols that have been employed previously by other groups in order to determine pK_a values [3–5].

Each model system was equilibrated in the protonated state for 5–10 ps without any constraint. Starting from those simulations, constrained AIMD runs were performed each for an additional 15–20 ps (30,000–40,000 steps (see Supplementary Materials Tables S11 and S12)). The first 5 ps (10,000 steps) of each individual run were neglected in order to give the system time to equilibrate e.g., adopt to the imposed constraint. The convergence of each model system with respect to simulation time is given in the supporting information (see Supplementary Materials Tables S3–S5).

3.1. Model Systems

Simulations were conducted for the systems given in Table 1. pK_a values were not only calculated for transition metal complexes, but also for two small organic molecules with pK_a values in the same range as the molecules of interest. Thereby phenol serves as an internal standard which allows for direct comparison with pK_a values obtained by the same methodology [3].

Table 1. Model systems used in this study. N_w stands for the number of water molecules in the simulation cell. The calculated pK_a value is only given if the simulations found in the literature were obtained employing the Bluemoon methodology. The Ru complex bears a pentapyridine (Py5) ligand that is composed of two bipyridyl fragments linked to a fifth pyridyl via an sp^3 carbon. The fourth fragment connected to the latter is either a methyl (Me) or methoxy (OMe) group resulting in Py5Me or Py5OMe (see [7,8,51] for more details). Experimental pK_a values denoted with “*” were only available for the Py5Me ligand framework (see Supplementary Materials Figure S1 for a graphical representation of the catalysts).

Molecule	N_w	Side-Length [Å]	pK_a (exp.)	pK_a (calc.)
H ₂ O	128	15.6	14.0	–
H ₂ O	256	19.7	14.0	–
HCOOH	126	15.6	3.8 [52]	–
PhOH	123	15.6	10.0 [52]	9.7 [3]
[Ru(II)Py ₅ Me(H ₂ O)] ²⁺	112	15.6	~11 [7]	–
[Ru(II)Py ₅ OMe(H ₂ O)] ²⁺	112	15.6	~11 [7] *	–
[Ru(II)Py ₅ OMe(H ₂ O)] ²⁺	234	19.7	~11 [7] *	–
[Ru(II)Py ₅ OMe(H ₂ O)] ³⁺	112	15.6	~3 [7] *	–
[Ru(II)Py ₅ OMe(H ₂ O)] ³⁺	234	19.7	~3 [7] *	–

In our previous study we have investigated the mechanism of the water oxidation reaction catalyzed by [Ru(II)Py₅Me(H₂O)]²⁺ and [Ru(II)Py₅OMe(H₂O)]²⁺ listed in Table 1, from a kinetic and thermodynamic point of view employing state of the art DFT simulations [7,8]. We found that both ligand frameworks Py5OMe and Py5Me were virtually identical in terms of their thermodynamics and kinetics of the water-oxidation reaction, which is a not too surprising result as the replacement of a methyl-group by a methoxy-group at an sp^3 carbon is not expected to remarkably alter electronics or sterics at the metal center. However, experimentally, the catalytic activity between the two ligands was found to be rather different, which was attributed to a rapid halide substitution at the catalyst bearing a Py5Me ligand. The latter leads to a deactivation of the catalyst [7]. As mechanistic studies for the more active catalyst Py5OMe are still underway, we decided to choose it as a model system even though no experimental pK_a values are currently available. Based on our previous study we would not expect the thermodynamics of the two ligands and related pK_a values to differ significantly [7,53].

Therefore comparing the calculated pK_a value of the Py5OMe and Py5Me systems serves as a further validation of the method.

3.2. Error Analysis

The standard deviation of the average forces used to calculate the free energy difference according to Equation (1) is calculated by block averaging methods [54]. An upper limit for the standard deviation (σ) of the pK_a is obtained by calculating the free energy ΔF of both, the average force ($\langle\lambda\rangle$) and the average force plus its standard deviation i.e., ($\langle\lambda\rangle + \sigma_\lambda$) [36].

4. Results and Discussion

4.1. Convergence of the AIMD Simulations

For our comparison of the post-processing methods we ran constrained AIMDs for the systems described in Section 3.1. As a constraint we chose the distance of the acidic proton from the acidic group ($d(A-H)$), which we scanned in steps of 0.1 Å over a range from 0.9 Å to 1.6 Å. The constraint was primarily chosen for its simplicity, which avoids additional parameters, i.e., the explicit definition of the proton accepting molecule. Further, Equation (1) holds only for the distance constraint, otherwise correction terms are necessary (see Equation (2)) [33]. For most of the systems, proton hopping is observed for $d(A-H)$ distances larger than 1.5 Å, which made the scanning of distances larger than 1.6 Å obsolete. In particular since large values of $d(A-H)$ do not necessarily describe the distance between the acidic group and the initially formed hydronium, since the latter potentially loses its one of its proton to other solvent molecules.

An exemplary PMF profile of PhOH is shown in Figure 1. Error bars on the average forces were obtained by block averaging methods. The absolute value of those standard deviations is in the range of 0.5 to 1.3 kcal/mol, which corresponds to 0.3 to 0.9 pK_a units. The PMF profiles of all the other model systems can be found in the Supplementary Materials Figures S2–S9.

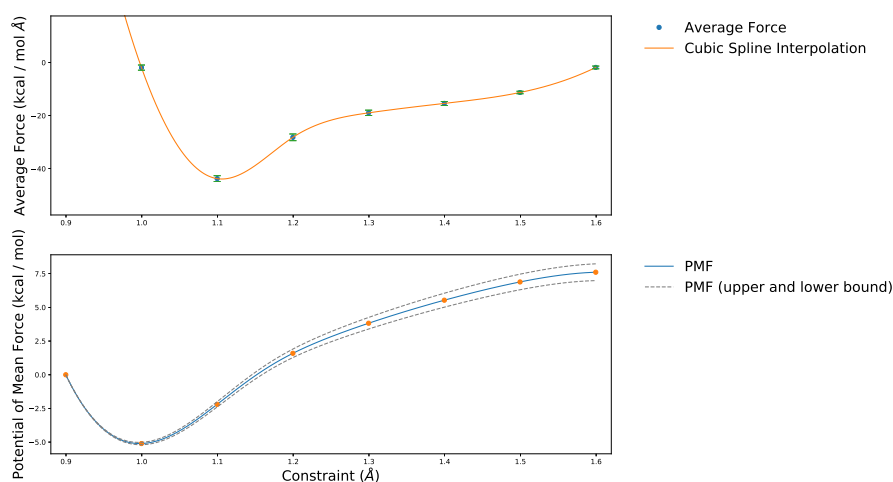


Figure 1. (top): Average force ($\langle\lambda\rangle$) acting on the constraint for the PhOH model system, constraining the A–H bond. (bottom): Potential of mean force, i.e., free energy obtained by integrating the average forces.

The convergence of the force acting on the constraint can be seen in Figure 2. Each of the traces represents a single point in the top part of Figure 1. Towards larger values of the constraint the fluctuations start to oscillate around zero, highlighting the fact that the A–H bond has been broken.

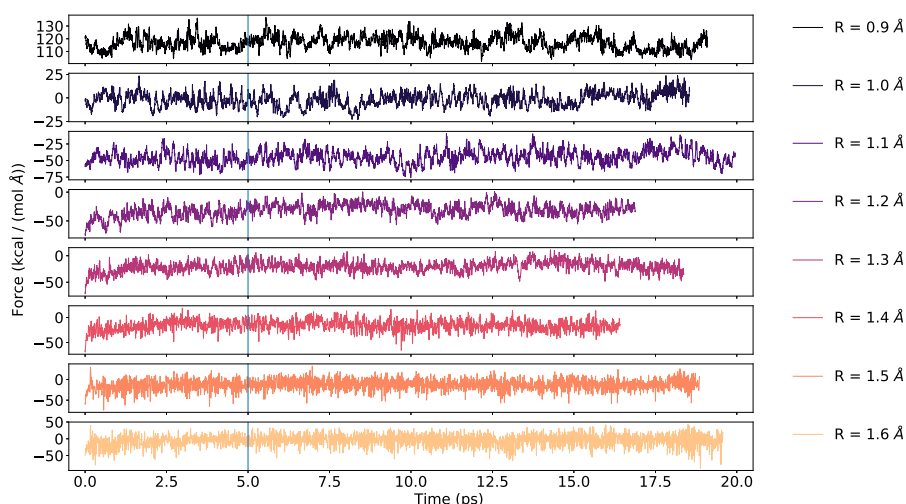


Figure 2. Force (λ) acting on the constraint—here for PhOH at a constrained $d(A-H)$. The vertical line at 5.0 ps marks the equilibration time in relation to the production run.

The autocorrelation function of the force acting on the constraint is used to determine the optimal block size for the average which is in the range of 0.5 to 1 ps (see Figure 3). The force appears to be heavily correlated for the constraints ≤ 1.3 Å which corresponds to the region where the A–H bond is broken (see Figure 2). Ivanov et al. further analyzed those autocorrelation functions in order to elucidate the bond breaking process [4]. Since the thermostat modulates the autocorrelation function, simulations in the micro-canonical ensemble (NVE) would be required which are beyond the scope of the current work.

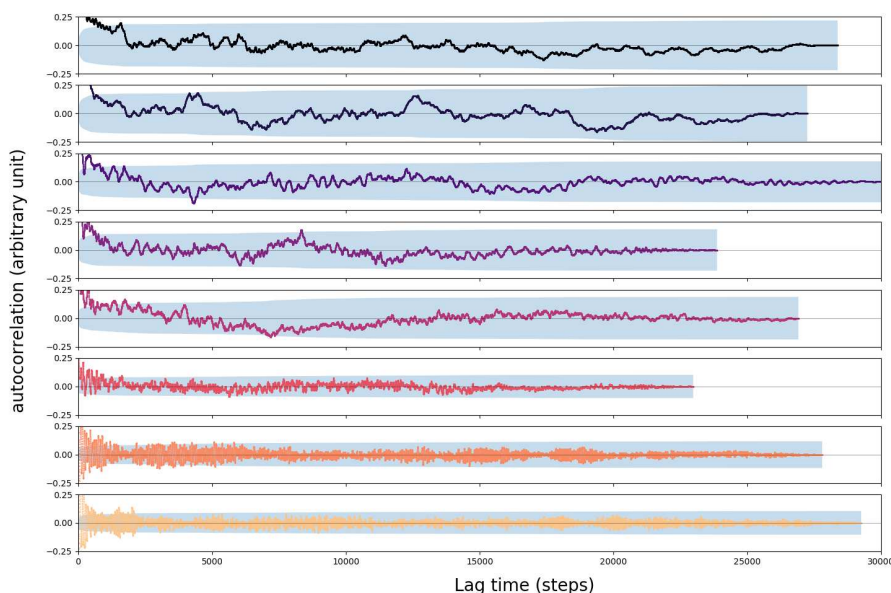


Figure 3. Autocorrelation function of the force acting on the constraint. From top to bottom the constraint increases by 0.1 Å, starting from 0.9 Å.

4.2. Reference System

In order to calculate the pK_a value according to the “relative” or “probabilistic” method, the simulation of water is required. We determined a cutoff radius R_c of 1.24 Å according to Equation (9) (see Figure 4). The same value was obtained for the two simulation cells containing either 128, or 256 water molecule (see Supplementary Materials Figure S17), which is in good agreement with 1.22 Å, respectively, 1.28 Å reported in literature [6,31,32]. As already reported by others, strong bases

such as OH^- tend to be reprotonated by the solvent. This is also the case in our simulations. Starting from a $d(\text{O}-\text{H})$ of 1.5 Å, we were able to observe the reprotonation of the OH^- moiety (see Figure 5). As discussed earlier, choosing a different collective variable could circumvent this issue.

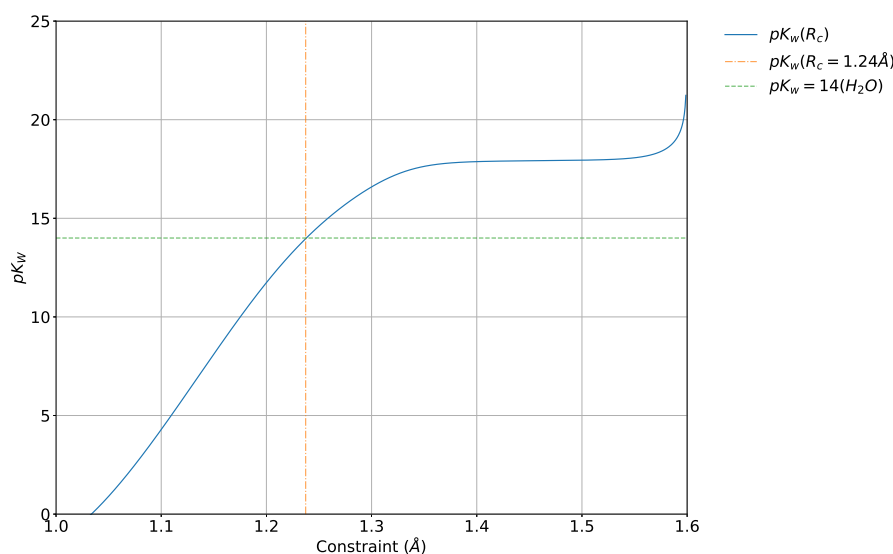


Figure 4. Determination of R_c from simulation of water, by fitting to the experimental value. The simulations were carried out in a cubic box with a side length of 15.6406 Å.

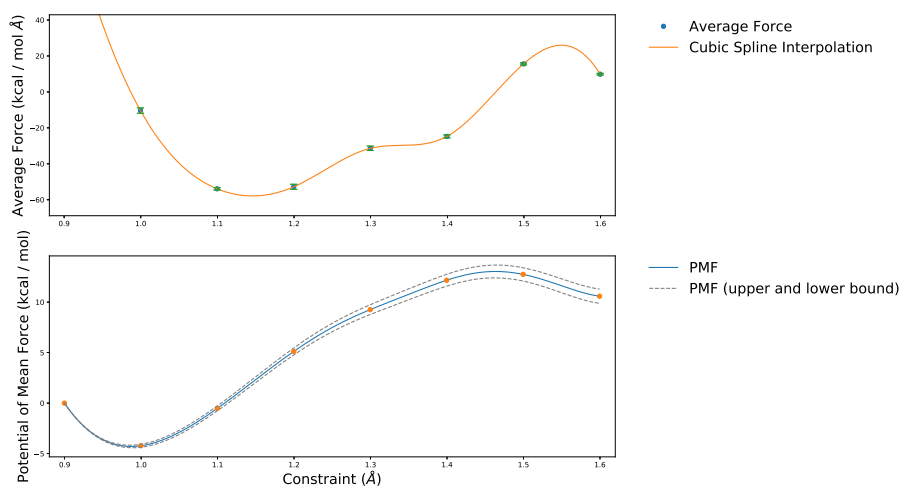


Figure 5. Autodissociation of H_2O (**top**): Average force acting on the constraint. (**bottom**): Free energy obtained by integrating the average forces. Note the drop in free energy at 1.5 Å is caused by the reprotonation of OH^- .

In the following we will present the pK_a values calculated based on the protocol described beforehand.

4.3. Overview of Calculated pK_a Values

In Table 2 the pK_a values obtained with the three simulation protocols are given. In general we find that the “absolute” protocol (see Equation (5)) underestimates the pK_a values compared to the experiment by about 1–2 pK_a units. pK_a values obtained by the relative protocol on the other hand are an overestimation by about two pK_a units. The best agreement is achieved with the probabilistic protocol where in particular pK_a values in the range of 10–11 are accurately reproduced. Hereby $[\text{Ru(III)Py}_5\text{OMe(H}_2\text{O)}]^{3+}$ is somewhat of an outlier with the largest difference compared to the experiment by about two pK_a units. As the only difference between $[\text{Ru(II)Py}_5\text{OMe(H}_2\text{O)}]^{2+}$ and

$[\text{Ru(III)Py}_5\text{OMe(H}_2\text{O)}]^{3+}$ is the charge of the system, we reasoned that the simulation cell might be too small for such highly charged species. The latter was verified by a set of simulations in a bigger simulation cell (see Table 3).

Table 2. All results presented here are calculated at 320 K, for a cubic box with side length of 15.6406 Å and a cutoff $R_C = 1.24$ Å, over a trajectory of about 20 ps (where the first 5 ps were not included in the evaluation). The standard deviation is calculated using the block average method with a block size of 1 ps; (a) absolute, (b) relative, (c) probabilistic protocols.

Molecule	pK _a (exp.)	pK _a ^(a)	pK _a ^(b)	pK _a ^(c)
H ₂ O	14.0	—	—	—
HCOOH	3.8 [52]	2.7 ± 0.5	6.7 ± 0.5	4.2 ± 0.6
PhOH	10.0 [52]	8.7 ± 0.3	12.5 ± 0.5	10.7 ± 0.4
[Ru(II)Py ₅ Me(H ₂ O)] ²⁺	~11 [51]	9.8 ± 0.4	13.7 ± 0.3	11.2 ± 0.4
[Ru(II)Py ₅ OMe(H ₂ O)] ²⁺	~11 [51]	9.3 ± 0.4	13.3 ± 0.6	11.1 ± 0.4
[Ru(III)Py ₅ OMe(H ₂ O)] ³⁺	~2.5 [51]	3.1 ± 0.4	7.1 ± 0.4	4.5 ± 0.5

The larger simulation cell slightly improves the agreement between the calculated pK_a values using the relative protocol and the experiment. However, there is no systematic improvement of the pK_a values with the system size, independent of the overall charge. Due to the significantly higher computational cost, we could not obtain the same level of convergence as compared to the smaller system. This can be seen from the shorter trajectories (see Supplementary Materials Tables S7 and S8).

Table 3. All results presented here are calculated at 320 K, for a cubic box with a side length of 19.7340 Å and a cutoff $R_C = 1.24$ Å over a trajectory of 10–15 ps (where the first 5 ps were not included in the evaluation). The standard deviation is calculated using the block average method with a block size of 1 ps; (a) absolute, (b) relative, (c) probability protocols.

Molecule	pK _a (exp.)	pK _a ^(a)	pK _a ^(b)	pK _a ^(c)
H ₂ O	14.0	—	—	—
[Ru(II)Py ₅ OMe(H ₂ O)] ²⁺	~11 [51]	10.1 ± 0.5	11.5 ± 0.5	12.7 ± 0.7
[Ru(III)Py ₅ OMe(H ₂ O)] ³⁺	~2.5 [51]	3.1 ± 0.3	4.6 ± 0.3	4.3 ± 0.4

4.4. Deuterated Solvent

The use of deuterated solute and solvent i.e., setting the mass of hydrogen atoms to 2 a.m.u may have a profound impact on calculated pK_a values. In principle all values presented in Tables 2 and 3 are pK_a^D values, i.e., pK_a values in D₂O instead of pK_a^H values, i.e., pK_a values in H₂O. Based on experiments, a correlation between pK_a^D and pK_a^H was reported already decades ago [55]. At first, the correlation was suspected to be linear only for pK_a values > 7 and constant for more acidic species [55]. Later, Delgado et al. experimentally determined a linear relation between pK_a^D and pK_a^H over the whole range of pK_a values [56]:

$$\text{pK}_a^D = 1.044\text{pK}_a^H + 0.32. \quad (10)$$

In a more recent study a detailed derivation of the linear relation between pK_a^D and pK_a^H has been presented by Krężel and Bal [57]:

$$\text{pK}_a^H = 0.929\text{pK}_a^{H^*} + 0.41, \quad (11)$$

where pK_a^{H*} is the pK_a value determined in a D₂O solution by a pH-meter which was calibrated by H₂O. Conversion to pK_a^D is achieved by adding the empirically determined constant of 0.4 to pK_a^{H*} [57]:

$$\text{pK}_a^D = \text{pK}_a^{H^*} + 0.4. \quad (12)$$

Combining Equations (11) and (12) and solving for pK_a^D results in:

$$pK_a^D = 1.076pK_a^H - 0.041, \quad (13)$$

which is of the same mathematical form as Equation (10).

Before employing either Equation (10) or (13) to convert pK_a^D to pK_a^H values, some additional alterations to the post-processing procedure have to be made, since some of them include an explicit reference to H_2O respectively its pK_w value.

For the probabilistic method, the cut-off radius R_c has to be redetermined since the pK_w^D of D_2O is 14.951 (25 °C) [58]. The obtained values for R_c are 1.26 Å, respectively 1.25 Å for the two simulation cells (see Supplementary Materials Figures S18 and S19). The pK_a^D values obtained with the cut-off R_c determined for D_2O were converted to pK_a^H values (see Tables 4 and 5).

Table 4. All results presented here are calculated at 320 K, for a cubic box with a side length of 15.6406 Å, over a trajectory of about 20 ps (where the first 5 ps were not included in the evaluation). The pK_a values were calculated using the probabilistic method for a R_c value of 1.26 Å determined for D_2O . The pK_a^H (a) was obtained referencing the calculations to H_2O i.e., a R_c of 1.24 Å. The pK_a^D values were converted to pK_a^H values according to Equation (10) (b), respectively Equation (13) (c).

Molecule	pK_a (exp.)	pK_a^H (a)	pK_a^D	pK_a^H (b)	pK_a^H (c)
H_2O	14.0	—	—	—	—
HCOOH	3.8 [52]	4.2	4.3	3.8	4.0
PhOH	10.0 [52]	10.7	11.2	10.4	10.5
$[Ru(II)Py_5Me(H_2O)]^{2+}$	~11 [51]	11.2	12.0	11.2	11.2
$[Ru(II)Py_5OMe(H_2O)]^{2+}$	~11 [51]	11.1	11.8	11.0	11.0
$[Ru(III)Py_5OMe(H_2O)]^{3+}$	~2.5 [51]	4.5	4.6	4.1	4.3

Table 5. All results presented here are calculated at 320 K, for a cubic box with a side length of 19.7340 Å, over a trajectory of about 20 ps (where the first 5 ps were not included in the evaluation). The pK_a values were calculated using the probabilistic method for a R_c value of 1.25 Å determined for D_2O . The pK_a^H (a) was obtained referencing the calculations to H_2O i.e., a R_c of 1.24 Å. The pK_a^D values were converted to pK_a^H values according to Equation (10) (b), respectively Equation (13) (c).

Molecule	pK_a (exp.)	pK_a^H (a)	pK_a^D	pK_a^H (b)	pK_a^H (c)
H_2O	14.0	—	—	—	—
$[Ru(II)Py_5OMe(H_2O)]^{2+}$	~11 [51]	12.7	13.1	12.2	12.2
$[Ru(III)Py_5OMe(H_2O)]^{3+}$	~2.5 [51]	4.3	4.4	3.9	4.1

The probabilistic pK_a^H values obtained by applying the conversion schemes discussed above are very similar to pK_a values determined by referencing our calculations to H_2O instead of D_2O . The difference when converting the pK_a^D values either according to Equation (10) or Equation (13) is negligible.

For pK_a^D values, respectively pK_a^H values derived from the latter, calculated either by the absolute or relative method see Supplementary Materials Tables S7–S10. For the relative protocol, the overestimation pK_a^H values is reduced by about 1–2 units. However, no systematic improvement is achieved as in particular the pK_a^H values for the acidic compounds were still significantly overestimated. Further, the results for the large simulation cell deteriorate. The agreement between the experimental and calculated pK_a^H values using the absolute protocol decreased by 0.1 to 0.6 units upon converting pK_a^D to pK_a^H values.

Taking into account the multitude of empirical factors required to convert the pK_a^D values led to the conclusion that the referencing pK_a values to H_2O is acceptable. This is in particular true for the probabilistic method. The validity of this conclusion could in principle be checked by repeating all the simulations with H_2O instead of D_2O . With a large enough test set, it would also be possible to adjust

equation of the linear relation to the employed methodology. However this is beyond the scope of the current work.

In the following we are going to highlight the dependence of the three methods on the cut-off radius (R_c).

4.5. Absolute and Probabilistic pK_a —Dependence on R_c

In Figure 6 both the absolute as well as the probabilistic pK_a values are shown as a function of the constraint (see Supplementary Materials Figures S11–S17 for plots for the other model systems). The choice of R_c is obviously crucial (see Figure 6). In order to illustrate the influence of R_c , pK_a values were also calculated with R_c values reported in literature (see Supplementary Materials Tables S1 and S2). Some systems are remarkably independent of R_c while for others they spread over a range of almost 3 pK_a units. This suggests that it is crucial to determine R_c with exactly the same settings as the systems of interest, rather than to rely on an previously published value.

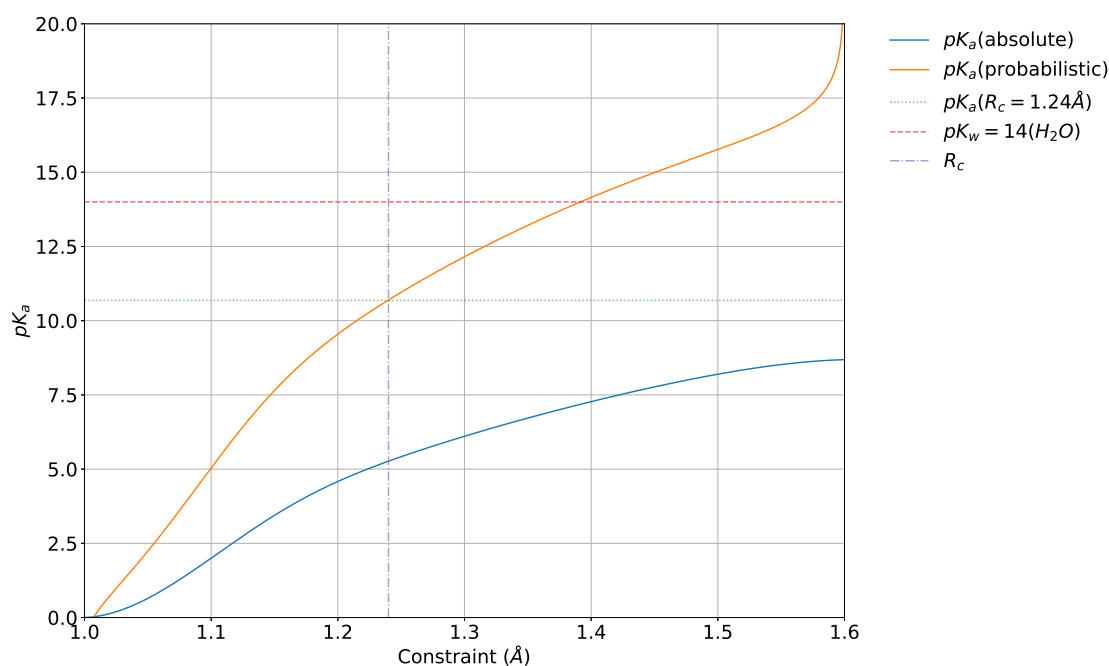


Figure 6. pK_a values calculated for PhOH using the absolute and probabilistic method. The latter is strongly dependent on the choice of R_c , even a change by 0.01 Å might result in change of up to 0.5 pK_a unit.

4.6. Relative pK_a

As for the probabilistic protocol, the dependency of the relative pK_a on R_c was investigated. As expected, the pK_a values calculated by Equation (6) show an asymptotic behavior towards larger values of R_c [4] (see Figure 7). The latter suggests that large values of R_c might be neglected in the evaluation. Indeed the results can be tuned i.e., lowered by 1 pK_a unit, if only constraints between 0.9 and 1.4 Å are considered (see Supplementary Materials Table S6). Nonetheless the results for the acidic compounds are still overestimated with 5.8 and 6.2 for HCOOH, respectively $[\text{Ru(III)Py}_5\text{OMe(H}_2\text{O)}]^{3+}$. Similar inconsistencies when applying the relative pK_a protocol to lumiflavins have also been reported by Kiliç et al. [2].

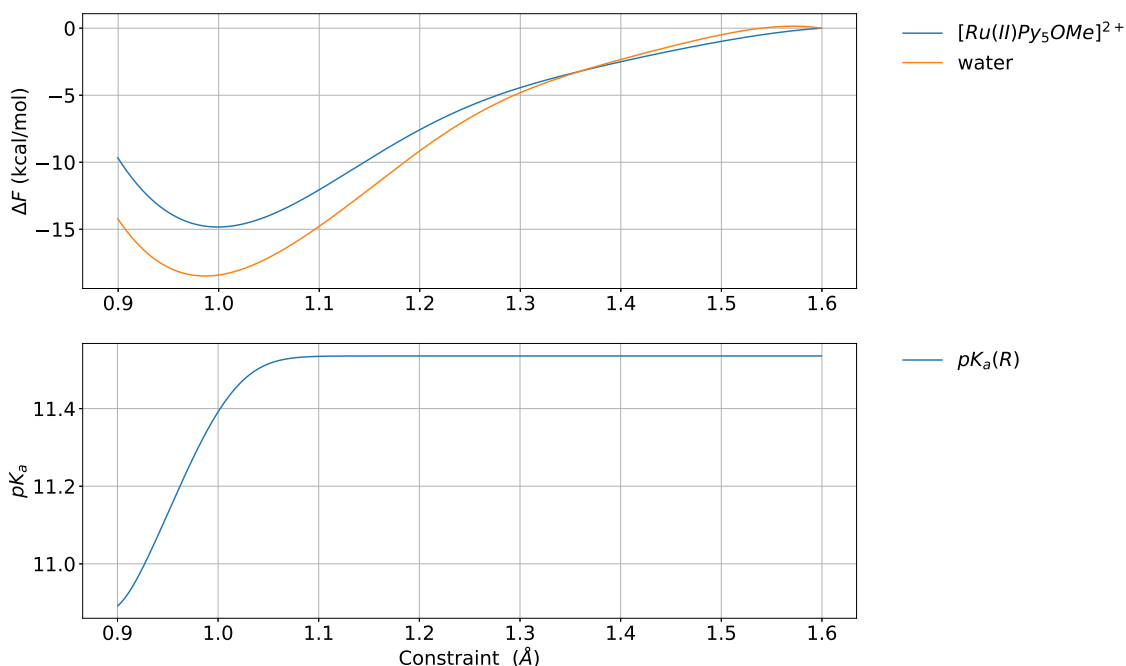


Figure 7. Relative pK_a as a function of $d(A-H)$ according to Equation (6), the value asymptotically approaches a constant value.

5. Summary and Conclusions

In summary, we have investigated the *Bluemoon* methodology and its various post-processing methods in order to determine pK_a values previously only applied to small organic molecules and transition metal aqua complexes. Our simulation cells with 128 respectively 256 water molecules were considerably larger than the ones previously presented in literature. This highlights the robustness and applicability of said protocol to larger chemically interesting systems, in particular in the context of water oxidation catalysts such as the here presented $Ru(Py_5Me)$ and $Ru(Py_5OMe)$ catalysts, for which we found, as expected, both qualitative and quantitative similar pK_a values independent of the applied post-processing method.

When comparing the three post-processing methods suggested in literature (1) absolute, (2) relative and (3) probabilistic pK_a (all referenced to H_2O), we find that method 1 and 3 are able to quantitatively reproduce experimental values with an accuracy of about 1 pK_a unit. In case of method 1 this is rather surprising as there is no guarantee that the free energy levels off within the scanned range of the constraint. Method 2 appears to at least qualitatively reproduce experimental pK_a values, however there seems to be no necessity to use said approach, as it requires exactly the same set of calculations as method 3 which performed the best within our test set. This conclusion also holds if one assumes that pK_a^D instead of pK_a^H values were calculated. For the sake of consistency we have only applied a very simple constraint i.e., the A–H distance. While this choice was fine for our test-set, there might be cases where more complex constraints are necessary, in particular if the conjugated base is very strong.

The overall accuracy of pK_a values calculated by the *Bluemoon* methodology using a simple distance constraint lies between 1–3 pK_a units. However if the computational settings are tailored in order to reproduce relevant experimental reference values, the accuracy might be increased. Overall it appears that both methods 2 and 3 slightly overestimate small pK_a values while large pK_a values are reproduced with high fidelity. This issue should be addressed in an extended benchmark study before one attempts to accurately predict low absolute pK_a values.

Further we want to highlight the importance of a sufficiently large simulation cell when investigating highly charged systems such as water oxidation catalysts with different oxidation

states. While the influence on the calculated pK_a values was found to be minor, only a large enough simulation cell can guarantee that there are no spurious interactions between the solute and its mirror image in the neighboring simulation cells.

Supplementary Materials: The following are available online at <http://www.mdpi.com/2304-6740/7/6/73/s1>, Manuscript.pdf (Figures S1 (Lewis structure of $[\text{Ru}(\text{II})\text{Py}_5\text{R}(\text{H}_2\text{O})]^{2+}$), Figures S2–S9 (Potentials of mean force as a function of the constraint - for all systems), Figures S10–S19 (Absolute and probabilistic pK_a values as a function of the constraint - for all systems), Tables S1–S5 (Convergence of pK_a with respect to simulation time), Tables S7–S10 (pK_a^D values converted to pK_a^H values for the absolute and relative protocol), Tables S11 and S12 (Summary of simulation times per system/constraint), the following CP2K files: .inp, .ener, .xyz (only start structure), .LagrangeMultLog (forces) are available for each calculation.

Author Contributions: M.S. and S.L.; methodology, M.S.; software, M.S.; validation, M.S. and S.L.; formal analysis, M.S.; investigation, M.S.; resources, S.L.; writing—original draft preparation, M.S.; writing—review and editing, S.L.; visualization, M.S.; supervision, S.L.

Funding: The work has been supported by the University of Zurich Research Priority Program “Solar Light to Chemical Energy Conversion” (LightChEC) and the Swiss National Science Foundation (grant no. PP00P2_170667). We thank the Swiss National Supercomputing Center and the Platform for Advanced Computing in Europe for computing resources (project ID: s745 and s788).

Acknowledgments: Mauro Schilling would like to state his gratitude towards Richard A. Cunha for the fruitful discussions.

Conflicts of Interest: The authors declare no conflict of interest.

Abbreviations

The following abbreviations are used in this manuscript:

MDPI	Multidisciplinary Digital Publishing Institute
DOAJ	Directory of open access journals
TLA	Three letter acronym
LD	Linear dichroism

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